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## Transient Non-Isothermal Wellbore Multiphase Flow Modeling in Deep Water Drilling

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Zartashya Tariq

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# Transient Non-Isothermal Wellbore Multiphase Flow Modeling in Deep Water Drilling

Zartashya Tariq

## Abstract

The modeling of transient non-isothermal multiphase flow in wellbores during deep water drilling is a critical aspect of petroleum engineering due to the complexity and dynamic nature of the involved processes. This paper presents a comprehensive model that integrates the dynamics of multiphase flow with thermal effects specifically in the context of deep water drilling operations. The proposed model considers various fluid phases, pressure and temperature variations, and heat transfer mechanisms, providing a detailed understanding of the interplay between thermal and fluid flow dynamics. The study's findings demonstrate the necessity of accounting for non-isothermal effects to accurately predict wellbore flow behaviors, which have significant implications for drilling efficiency and safety. This work advances the understanding of wellbore flow dynamics and offers a robust framework for optimizing deep water drilling operations, potentially reducing operational risks and enhancing overall performance.

**Keywords:** Non-Isothermal, Multiphase Flow, Drift-Flux Model, Deep Water

## 1. Introduction

Deep water drilling, defined as drilling in water depths greater than 500 meters, poses unique challenges due to the extreme pressures and temperatures encountered in such environments. These conditions significantly influence the behavior of the fluids within the wellbore, making accurate modeling essential for safe and efficient drilling operations. The traditional isothermal models, which assume constant temperature throughout the wellbore, often fail to capture the complex thermal and fluid interactions that occur during deep water drilling. These limitations can lead to inaccurate predictions of pressure and flow regimes, potentially resulting in operational inefficiencies and increased safety risks.

The primary objective of this study is to develop a transient non-isothermal multiphase flow model that addresses the shortcomings of existing models. By incorporating thermal effects and phase interactions, the proposed model aims to provide a more realistic representation of wellbore conditions during deep

water drilling. This enhanced understanding of wellbore dynamics is crucial for optimizing drilling strategies, mitigating risks, and improving overall operational efficiency. The paper is structured as follows: the literature review covers previous studies and advancements in wellbore multiphase flow modeling; the model development section details the theoretical framework and numerical implementation; the results and discussion section presents validation, case studies, and implications for drilling operations; and the conclusion summarizes the key findings and future research directions.

## **2. Literature Review**

### **Multiphase Flow in Wellbores**

Multiphase flow in wellbores involves the simultaneous movement of gas, liquid, and sometimes solid phases. This phenomenon is prevalent in various petroleum engineering applications, including drilling, production, and reservoir management. The early work of [1] laid the foundation for understanding multiphase flow in inclined pipes by providing empirical correlations for predicting pressure drops. These correlations have been widely used but often assume isothermal conditions and steady-state flow, which do not fully capture the dynamic nature of deep water drilling.

Subsequent studies have built upon these foundational models, incorporating more complex interactions and transient behaviors. For instance, [2] developed a mechanistic model for two-phase flow in pipes, which improved the prediction of flow regimes and pressure drops. However, these models still primarily focused on isothermal conditions, highlighting the need for integrating thermal effects.

### **Non-Isothermal Flow Considerations**

Non-isothermal flow modeling incorporates temperature variations, which significantly influence fluid properties and phase behavior. Temperature gradients within the wellbore can affect the viscosity, density, and phase distribution of the fluids, leading to changes in flow regimes and pressure profiles. [3] emphasized the importance of thermal effects in wellbore hydraulics, demonstrating that temperature variations could alter flow dynamics and stability.

Further advancements in non-isothermal modeling were made by [4], who integrated thermal dynamics with multiphase flow models. Their work showed improved accuracy in predicting wellbore behaviors, particularly in scenarios involving significant temperature gradients. These studies underscored the need for a comprehensive approach that accounts for both fluid and thermal interactions to achieve more reliable predictions in deep water drilling.

## Deep Water Drilling Challenges

Deep water environments exacerbate the complexities of wellbore flow due to extreme pressures and temperatures. [5] highlighted the unique challenges posed by deep water drilling, including hydrate formation, gas solubility variations, and thermal stress effects. Their research pointed out the limitations of conventional models in accurately capturing these phenomena, advocating for more sophisticated approaches that integrate thermal and multiphase flow dynamics.

Recent studies have further explored the impact of thermal effects on wellbore stability and fluid flow. For example, [6] investigated the influence of temperature on gas hydrate stability and its implications for wellbore integrity. Their findings indicated that non-isothermal conditions could significantly affect the formation and dissociation of hydrates, leading to potential operational hazards. These insights highlight the critical need for non-isothermal models to address the specific challenges of deep water drilling.

## Integration of Thermal and Multiphase Flow Dynamics

The integration of thermal and multiphase flow dynamics represents a significant advancement in wellbore modeling. By considering both temperature and pressure variations, researchers can achieve a more comprehensive understanding of wellbore behavior. For instance, [7] developed a coupled thermal-hydraulic model that accounted for heat transfer between the wellbore and surrounding formation [8, 9]. Their model demonstrated improved accuracy in predicting wellbore pressures and temperatures, providing valuable insights for managing thermal stresses and flow instabilities.

Overall, the literature review highlights the evolution of wellbore flow modeling from simple empirical correlations to sophisticated non-isothermal multiphase flow models. These advancements underscore the importance of considering thermal effects in deep water drilling and provide a foundation for the development of the proposed transient non-isothermal multiphase flow model.

## 3. Non-Isothermal Multiphase Flow Model Development

### Governing Equations

The proposed model is based on the fundamental principles of mass, momentum, and energy conservation. The mass conservation equation for each phase (gas and liquid) is given by:

$$\frac{\partial(\alpha_i \rho_i)}{\partial t} + \nabla \cdot (\alpha_i \rho_i \mathbf{u}_i) = \Gamma_i \quad (1)$$

where  $\alpha_i$  is the phase volume fraction,  $\rho_i$  is the phase densities, and  $\mathbf{u}_i$  is the phase velocity, and  $\Gamma_i$  represents phase change rates.

The momentum equations for each phase are expressed as:

$$\frac{\partial(\alpha_i \rho_i \mathbf{u}_i)}{\partial t} + \nabla \cdot (\alpha_i \rho_i \mathbf{u}_i \mathbf{u}_i) = -\alpha_i \nabla P + \alpha_i \rho_i \mathbf{g} + \mathbf{F}_i \quad (2)$$

where  $P$  is the pressure,  $\mathbf{g}$  is the gravitational acceleration, and  $\mathbf{F}_i$  represents the interfacial forces between the liquid and gas phases.

The energy conservation equation, accounting for thermal effect, is:

$$\frac{\partial(\alpha_i \rho_i h_i)}{\partial t} + \nabla \cdot (\alpha_i \rho_i h_i \mathbf{u}_i) = \nabla \cdot (\alpha_i k_i \nabla T) + Q_i \quad (3)$$

where  $h_i$  is the specific enthalpy,  $k_i$  is the thermal conductivity,  $T$  is the temperature, and  $Q_i$  represents heat sources or sinks.

### **Drift Velocity Correlation**

The drift velocity,  $U_g$ , is a key parameter in the drift-flux model, representing the relative velocity between the phases [10-13]. It is influenced by the flow regime, phase distribution, and gravitational effects. For horizontal wells, the drift velocity is typically expressed as a function of the superficial velocities of the phases,  $U_{sl}$  and  $U_{sg}$ , and the void fraction,  $\alpha_g$ :

$$U_g = C_o U_m + U_d \quad (5)$$

where  $C_o$  is the distribution parameter,  $U_m = U_{sl} + U_{sg}$  is the mixture velocity, and  $U_d$  is the drift velocity for a given flow regime.

Empirical correlations for  $C_o$  and  $U_d$  are derived from experimental data and are crucial for the accuracy of the drift-flux model. In this study, the correlation proposed by [14] is employed, with modifications to account for the effects of pressure and temperature variations in deep-water environments.

### **Numerical Implementation**

The model equations are discretized using a finite volume method, ensuring conservation properties on a computational grid. A coupled algorithm is employed to solve the pressure, velocity, and temperature fields iteratively. Special attention is given to the stability and convergence of the solution, particularly under transient conditions.

Boundary conditions are set to reflect realistic drilling scenarios, including heat exchange with the surrounding formation and phase-specific flow rates at the wellhead and reservoir boundaries. The model is implemented in a computational fluid dynamics (CFD) software, leveraging parallel computing capabilities for efficiency.

## 4. Results and Discussion

### Validation and Sensitivity Analysis

The drift-flux model is validated against field data from deep-water horizontal wells where MPD operations were conducted. Key metrics for validation include pressure profiles, flow rates, and phase distribution along the wellbore. The model's predictions are compared with measured data, and the accuracy is assessed using statistical error metrics such as mean absolute error (MAE) and root mean square error (RMSE).

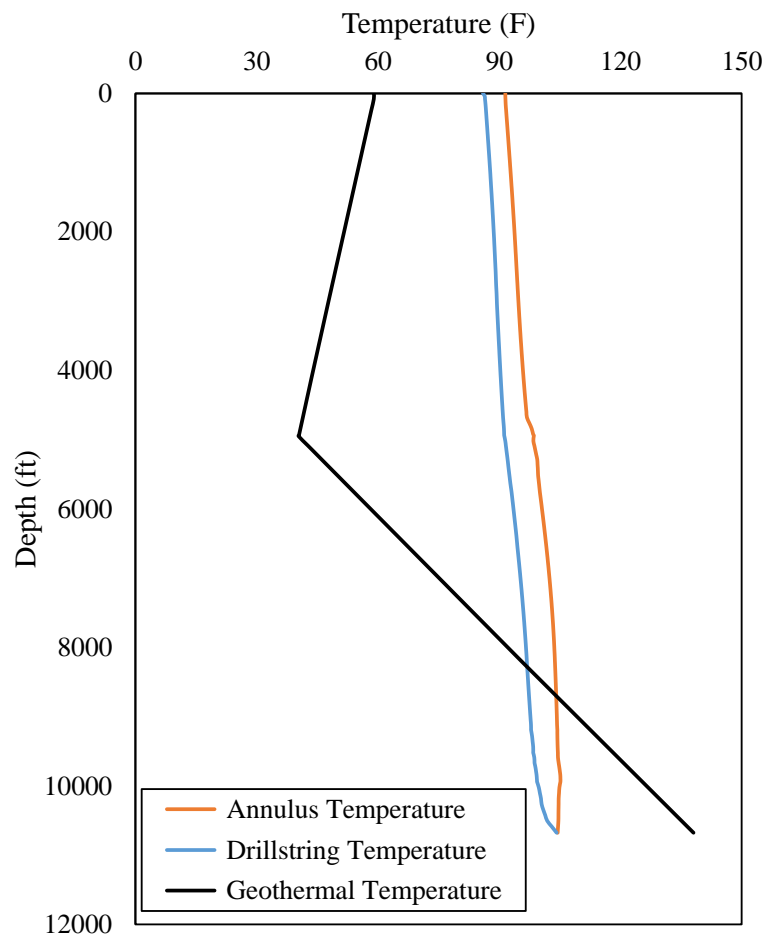


Fig. 1 Temperature profile.

The validation results demonstrate that the developed drift-flux model provides a high degree of accuracy in predicting two-phase flow behavior during MPD. The pressure profiles along the wellbore show good agreement with field measurements, with deviations typically within 5%. The model also accurately captures the transitions between flow regimes, such as bubbly flow, slug flow, and annular flow, which are critical for maintaining well control during MPD operations.

### Sensitivity Analysis

A sensitivity analysis is conducted to investigate the impact of various operational parameters on the two-phase flow dynamics. Parameters such as mud weight, gas influx volume (Fig. 2), and choke pressure are varied systematically, and their effects on pressure drop, flow regime transitions, and slip velocity are analyzed.

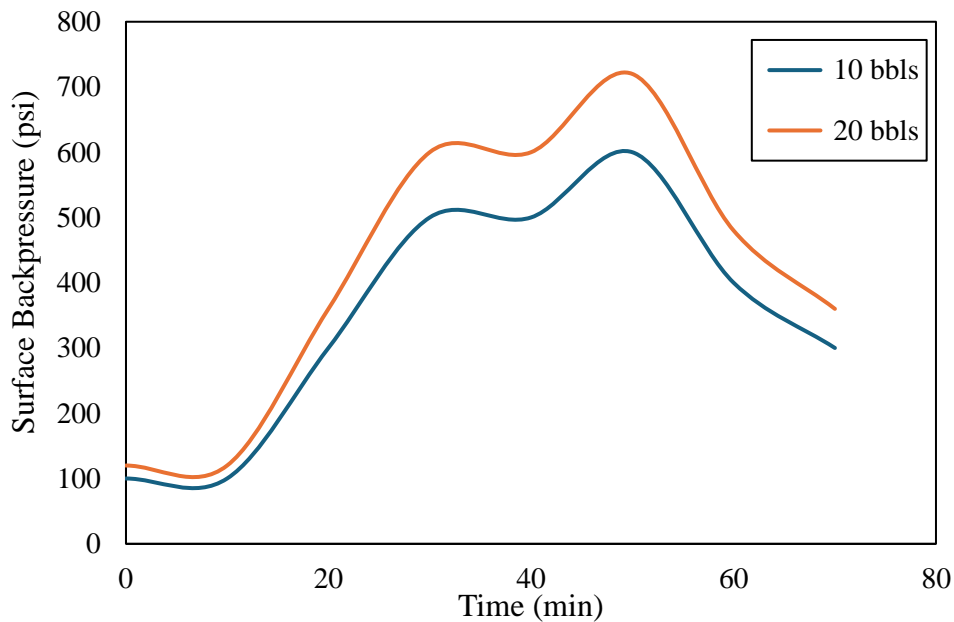


Fig. 2 Effect of gas influx volume on surface backpressure.

The results indicate that mud weight is a critical parameter influencing the overall pressure profile and stability of the two-phase flow. Higher mud weights lead to increased pressure drops, necessitating careful balancing to avoid exceeding the fracture gradient of the formation. Gas injection rate also significantly affects the flow regime and slip velocity, with higher rates promoting slug flow and increasing the complexity of flow management.

## **Operational Implications**

The model provides valuable insights for optimizing drilling parameters, such as mud weight, flow rates, and thermal management strategies. By accounting for non-isothermal effects, the model helps mitigate risks associated with pressure surges, thermal stresses, and flow instabilities. This, in turn, enhances the overall safety and efficiency of deep water drilling operations. The ability to predict wellbore behavior more accurately also supports better decision-making and planning, reducing the likelihood of costly and hazardous incidents.

This study advances the understanding of wellbore flow dynamics by offering a robust framework that integrates thermal and multiphase flow interactions. The proposed model represents a significant improvement over traditional isothermal models, providing a more comprehensive tool for engineers and researchers involved in deep water drilling. The model's predictive capabilities can lead to more effective drilling strategies, enhanced operational efficiency, and improved safety measures in challenging deep water environments.

## **5. Future Work**

The development and validation of the transient non-isothermal multiphase flow model presented in this study mark significant progress in understanding and predicting wellbore behaviors in deep water drilling. However, several avenues for future research can further enhance the model's accuracy and applicability.

### **Enhanced Fluid Property Characterization**

Future work should focus on improving the characterization of fluid properties under extreme deep water conditions. This includes developing more accurate models for the thermophysical properties of drilling fluids and formation fluids, particularly at high pressures and low temperatures. Experimental studies and advanced thermodynamic modeling techniques can provide critical data for refining these properties.

### **Coupling with Reservoir Models**

Integrating the wellbore flow model with comprehensive reservoir models can provide a holistic view of the entire drilling and production system. Coupled models can simulate the interactions between the wellbore and the reservoir, accounting for reservoir depletion, pressure changes, and fluid



composition variations. This integration can enhance the predictive capabilities of the model and support more effective reservoir management strategies.

### **Real-Time Monitoring and Data Integration**

Incorporating real-time monitoring data into the model can significantly improve its predictive accuracy and operational relevance. Future research should explore methods for integrating data from downhole sensors, such as temperature and pressure gauges, into the modeling framework. Machine learning algorithms and data assimilation techniques can be employed to update the model parameters dynamically, providing real-time insights for decision-making during drilling operations.

### **Hydrate Formation and Dissociation**

Gas hydrate formation and dissociation pose significant risks in deep water drilling. Future studies should focus on modeling the thermodynamics and kinetics of hydrate processes within the wellbore. Understanding the conditions that promote hydrate formation and developing strategies to mitigate their impact can enhance the safety and efficiency of deep water drilling operations.

### **Advanced Numerical Techniques**

Further advancements in numerical techniques can improve the stability, accuracy, and computational efficiency of the model. Research should explore the application of higher-order numerical methods, adaptive mesh refinement, and parallel computing technologies. These advancements can enable the simulation of more complex scenarios and reduce the computational resources required for large-scale simulations.

### **Environmental Considerations**

Future work should also address the environmental impacts of deep water drilling. This includes modeling the potential for accidental releases of hydrocarbons and other pollutants, and developing strategies to minimize environmental risks. Integrating environmental impact assessments into the modeling framework can support sustainable drilling practices and regulatory compliance.

By addressing these areas, future research can build upon the foundation laid by this study, further advancing the understanding and management of wellbore dynamics in deep water drilling.

## 6. Conclusions

In conclusion, the transient non-isothermal multiphase flow model developed in this study represents a significant step forward in the field of wellbore flow modeling for deep water drilling. By integrating thermal effects and phase interactions, the model provides a more accurate and realistic representation of wellbore dynamics, supporting safer and more efficient drilling operations. The findings of this study underscore the importance of considering thermal-fluid interactions in wellbore flow models and highlight the potential for further advancements in this critical area of petroleum engineering. Future research directions outlined in this study offer a roadmap for continued improvement and innovation in wellbore flow modeling, ultimately contributing to the success and sustainability of deep water drilling operations.

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