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Abstract

We have tried to investigate what is the effect of noisy image filtration with different wavelet transform and analyzing the image decomposition at level 7, image denoised at level 7 and reconstruction approximation at level 7 with wavelet transform approximation.

Keywords

Image De-composition, image denoised, wavelet transform, wavelet base.

1. Introduction:

The main object of image decomposition technique is to analyze the transformation of an image to transform various levels of images. Since in wavelet analysis the Daubechies wavelet, Haar & symlets wavelet will be the member of wavelet family. The decomposition technique of image means, the transformation of images in lo-pass & High-pass filtration image, In recent years many researchers have applied wavelet thersholding and threshold selection based technique for denoising image, decomposition image since wavelet thresholding is a suitable basis for extracting noisy signal, images from original image signal [7],[8].

2. Wavelet Family

We are introducing three types of wavelet, that is Daubechies wavelet (db), Haar wavelet and the symlets wavelet. Daubechies wavelet (db) was first developed in theory and construction of orthonormal wavelet with compact support. In Haar

wavelet the simplest analysis is based on the Haar scaling function which create the image building blokes are translations & dilations(height & width), this is the basic properties of Haar wavelets. The symlets wavelets belong to the wavelet family and it is the modified Daubechies wavelet (db) with increased symmetry.

3. Wavelet base

According to Daubechies wavelet the finite element in the time domain, the length of $\psi(t)$ is finite and its higher order element is

$$\int t^q \psi(t) dt = 0 \text{ When } q = 0 \text{ and } N \text{ is the natural value.}$$

So in the frequency domain, $\psi(t)$ and it has the zero point at ω and its integer displacement are orthogonal.

4. Continuous wavelet transform

Let $\psi \in L^2(\mathbb{R})$ and $\psi_{a,b}(t)$ is given by the equation based on the idea of wavelets as a family of function constructed from translation and dilation of a single function ψ , called the mother wavelet, then

$$\psi_{ab}(t) = \frac{1}{\sqrt{|a|}} \psi\left(\frac{t-b}{a}\right), \quad a, b \in \mathbb{R} \quad a \neq 0$$

..... (1)

Then the integral transform w_ψ defined on $L^2(\mathbb{R})$ by,

$$W_\psi[f](a,b) = (f, \psi_{a,b}) = \int_{-\infty}^{\infty} f(t) \overline{\psi_{a,b}(t)} dt$$

..... (2)

Is called the continuous wavelet transform of $f(t)$ [1].

5. Implementation methodology and the image analysis

We are using multi layer image decomposition with noisy image and it is analyzed in Matlab by wavelet family’s member like Daubechies wavelet, symlets & Haar etc. First we implement the noisy image i.e. butterfly image (172×175). Now we investigate the noisy image analysis with these three wavelet family member,

- (1) Daubechies wavelet (db).
- (2) Haar wavelet
- (3) Symlets wavelet

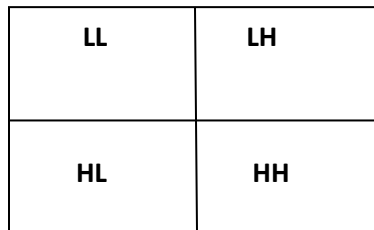
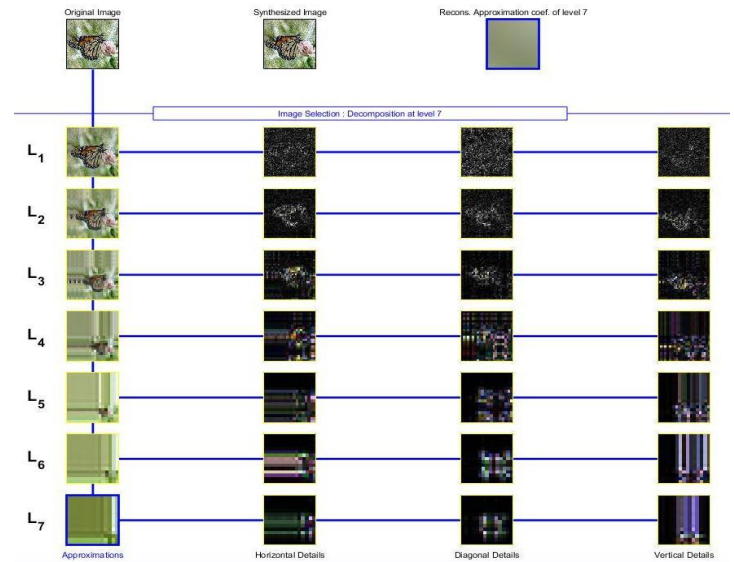


Figure: (A)

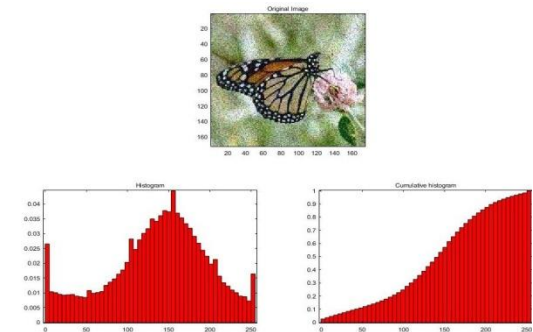
Now we see in figure (A) the decomposition level of the image stage 1 & filtration image will be high-high, high-low, low-high, & low-low frequency. That is basic method of analysis of image by using this type of filtration, denoising & decomposition [2].

(1) Analysis of Image transform and respective data structure with Daubechies wavelet (db)

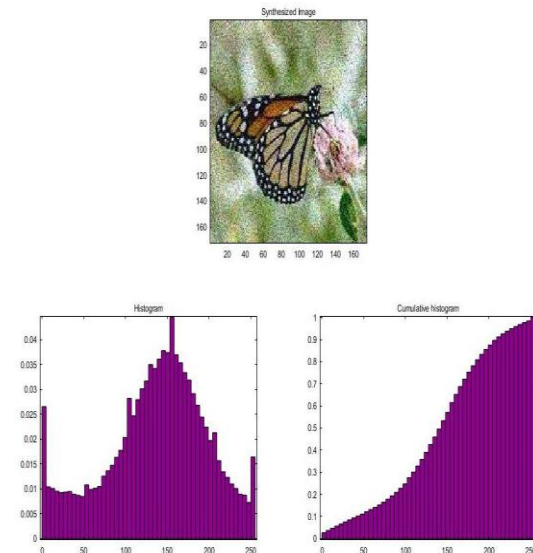
(a) Butterfly image structure of Daubechies wavelet decomposition level 7



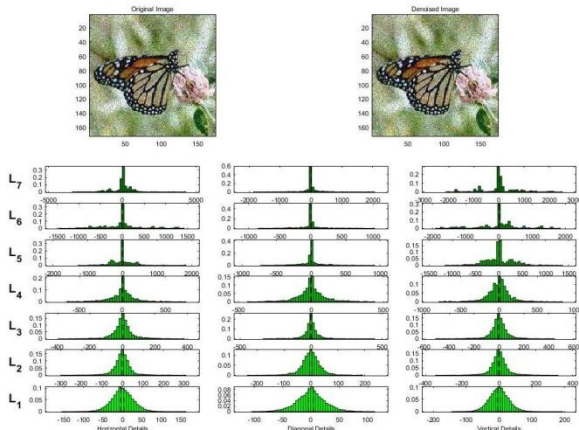
(b) Original image of butterfly with histogram & cumulative diagram (db) level 7



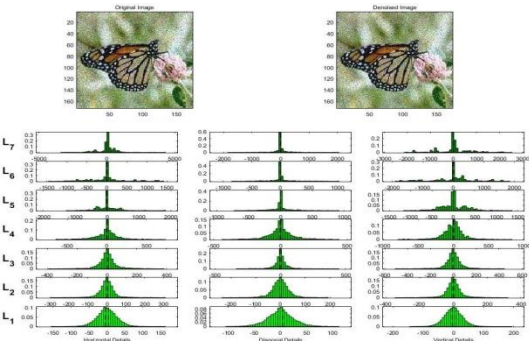
(c) Synthesized image of butterfly with histogram & cumulative diagram (db) level 7



(d) Original image of butterfly with denoised image statistics (db) level 7



(e) Synthesized image of butterfly with denoised image statistics (db) level 7



Analysis of the figure at a, b, c, d, e, of (1) above data due to Daubechies wavelet at Decomposition Level – 7 for image of noisy image butterfly

Data table (1.1)

S.no.	Functions	Thresholding level	Hard Threshold	Soft Threshold
1	L1	1	4.509	4.509
2	L2	2	4.247	4.247
3	L3	3	4.015	4.015

4	L4	4	3.828	3.828
5	L5	5	3.694	3.694
6	L6	6	3.61	3.61
7	L7	7	3.571	3.571

Data table (1.2)

Daubechies wavelet original image statistics

Mean	Median	Mean	Maximum	Minimum
136.7	143	155.6	255	0

range	Standard Deviation	Median Abs. Dev.	Mean Abs. Dev.	L1norm	L2norm	Maximum norm
255	60.21	38	47.81	1.234e+07	4.489e+04	255

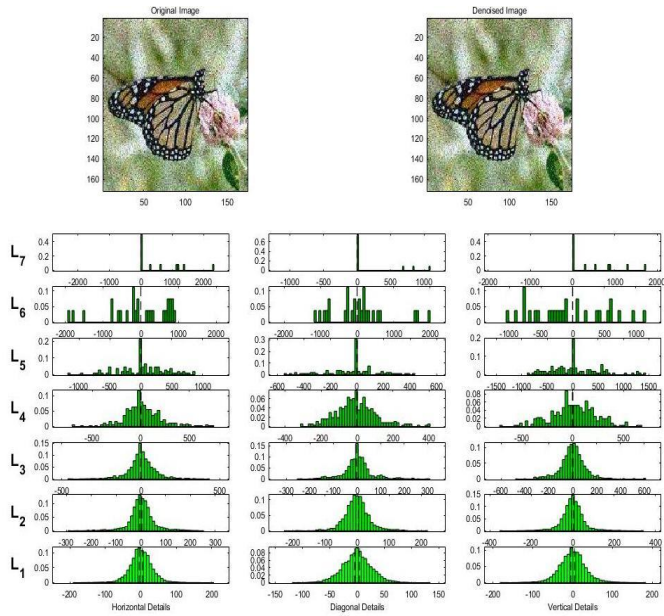
Thus the synthesized image statistics data are the same as mention above.

(2) Analysis of Image transform and respective data structure with Haar wavelet

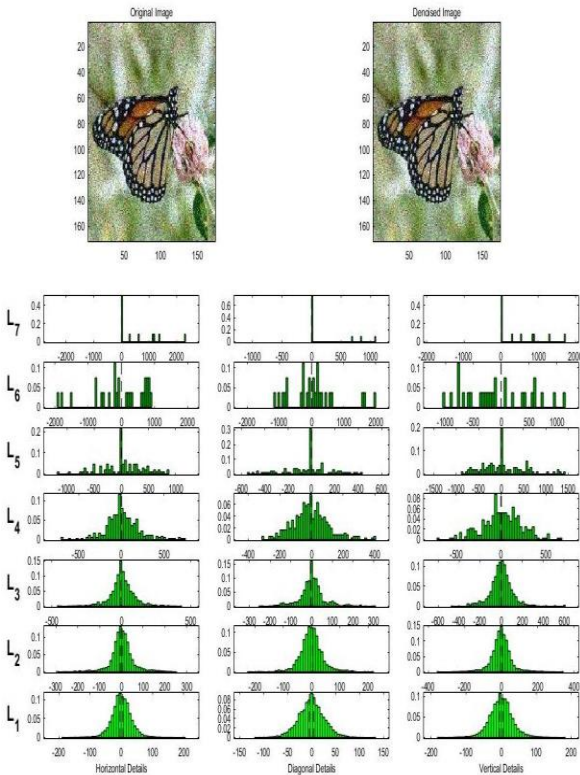
(f) Butterfly image by Haar wavelet decomposition level 7



(g) Original image of butterfly with denoised image statistics Haar level 7



(h) Synthesized image of butterfly with denoised image statistics Haar level 7



Analysis of the figure at f, g, h, of (2) above data due to Haar wavelet at Decomposition Level – 7 for image of noisy image butterfly

Data table (1.3)

S.no	Functions	Thresholding level	Hard Threshold	Soft Threshold
1	L1	1	4.479	4.479
2	L2	2	4.158	4.158
3	L3	3	3.816	3.816
4	L4	4	3.433	3.433
5	L5	5	3.06	3.06
6	L6	6	2.567	2.567
7	L7	7	2.229	2.229

Data table (1.4)

Haar wavelet original image statistics

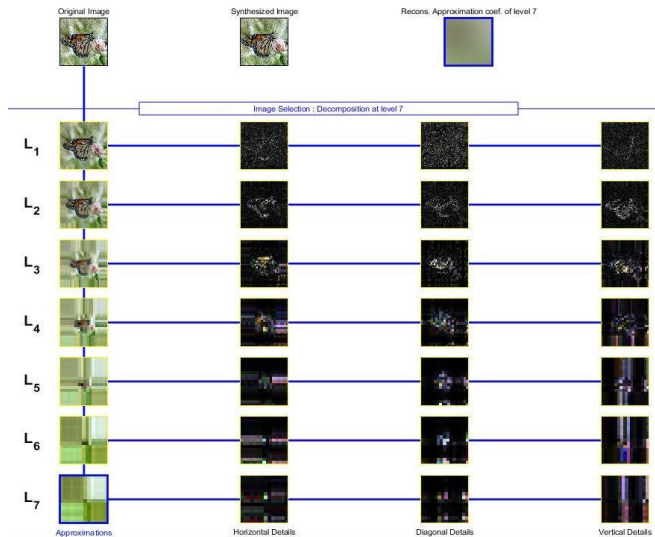
Mean	Median	Mean	Maximum	Minimum
136.7	143	155.6	255	0

range	Standard Deviation	Median Abs. Dev.	Mean Abs. Dev.	L1norm	L2norm	Max norm
255	60.21	38	47.81	1.234e+07	4.489e+04	255

Thus the synthesized image statics data will be same as mention above.

(3) Analysis of Image transform and respective data structure with Symlets Wavelet

(i) Butterfly structure of Symlets Wavelets decomposition level 7



Analysis of the figure at (i) of (3) above data due to symlets wavelet at Decomposition Level – 7 for image of noisy image butterfly

Data table (1.5)

S.n o.	Functions	Thresholding level	Hard Thresh	Soft Thresh
1	L1	1	4.509	4.509
2	L2	2	4.247	4.247
3	L3	3	4.015	4.015
4	L4	4	3.828	3.828
5	L5	5	3.694	3.694
6	L6	6	3.61	3.61
7	L7	7	3.571	3.571

**Data table (1.6)
Symlets wavelet original image statics**

Mean	Median	Mean	Maximum	Minimum
136.7	143	155.6	255	0

range	Standard Deviation	Median Abs. Dev.	Mean Abs. Dev.	L1norm	L2norm	Maximum norm
255	60.21	38	47.81	1.234e+07	4.489e+04	255

Thus the synthesized image statics data will be same as mention above.

6. Explanation & Result

In decomposition level 7, we analyzed the original image is transforming with the help of discrete wavelet transform and it's covert into HH, LH, HL, & LL. We see in Image 1(a), that applying inverse discrete wavelet transform in the decomposition at level 7, it converted into a synthesized image of butterfly and also the approximation details given in Image 1(a) it shows that the reconstruction approximation coefficients of level 7. In Image 1(d), the statistics of the decomposed image has been shown. Also in 1(e) the statistics of the denoised image of synthesized image has been shown at the data table (1.1).

In figure (1) first we take Daubechies wavelet applying at the butterfly image in decomposition level 7 it gives the function called L1, L2, L3, to L7 at thersholding level 1 to 7 therefore it's maximum hard thresholding level shown in L1 is 4.509 and it is similar value to soft thresholding at a certain fix point and also in [fig 1(a)] the function L7 approximation detailed at

Daubechies wavelet shows that the image of reconstructions approximation coefficients of level 7 and it gives the horizontal, diagonal & vertical detailing of the image of noisy butterfly. Now the original image of butterfly statistics decomposition at level 7, the histogram and commutative diagram shows the result in data table (1.2) therefore, the important part of the statistics value of butterfly image [Image. 1(b)] is as same as the image of [Image.1(c)] and also the values remains constant. Then the outcome of this image, the maximum deviation will be 255 db & minimum deviation will be zero db. Therefore L1 norm and L2 norm will be $1.234e+07$ & $4.489e+04$ since the maximum will be 255.

Now in figure(2) data analysis of butterfly image with Haar system the outcome statistics will be shown in data table (1.3) it shows the maximum decomposition L1- function will be hard thresh i.e. 4.479 & soft thresh will be remain same. Similarly in data table (1.4) the original and synthesized image of butterfly statistics histogram and commutative diagram remains constant as shown in the above data table (1.2) of Daubechies wavelet.

Again in figure (3) butterfly image applying with symlets wavelets we calculate the transforming of the image decomposition level 7, we analyzed in data table value remain as same as the given data table value (1.1) and (1.2) of Daubechies wavelet. That region symlets wavelet is nearly equal to Daubechies wavelet at the filtration of butterfly image at decomposition level 7.

7. Conclusion and future work

We have tried to analyze butterfly image with wavelet family and the comparative analysis has been done. Then we found in multilevel decomposition, reconstruction and filtering with noisy type of image, the Daubechies wavelet & symlets wavelet best for transformation of noisy image than other wavelet transform. In other hand the noisy image with Haar transform it will be not satisfies outcome analysis result than Daubechies wavelet & symlets wavelet. Therefore in future work with any type of noisy image with one or two dimension symlets & Daubechies wavelet will be perform continuously good as they have.

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